

Distance sampling: methods and applications

Covariates in detectability case study, Hawaiian amakihi

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This case study is intended to duplicate the findings shown in Section 5.3.2 of the book which duplicates the analysis presented by Marques et al. (2007). This document describes the analysis of these data both using the Distance GUI software as well as analysis in R.

1 Amakihi analysis using the Distance software

This set of data is included in the distribution of Distance as one of the *Sample Projects*. You can open this project (entitled *amakihi.zip*) in the *Sample project* directory underneath *My Distance projects* directory residing under *My Documents*. Open and extract the contents of the archived .zip file to any convenient location on your computer.

1.1 Data summary

When the project is unzipped and opens, have a brief look at the nature of the data using the **Data** tab. You will see fields corresponding to the description in Section 5.3.2.1. Specifically, check that the *Point labels* run from 1 to 41, representing the 41 point transects sampled. You can see from the *observation ID* column there are 1434 sighting in this dataset (not the 1485 noted in Section 5.3.2.1). Finally looking at the *Region ID* field you will find there are 7 “regions” corresponding to the 7 replicate surveys conducted that are represented in this project as temporal strata. Consequently the data are sorted by transect within region. Points are visited an equal number of times during each survey period, so the amount of survey effort is “1” for all points.

1.2 Analysis summary

Moving to the **Analysis** tab, you will find a set of 16 model definitions in the Project browser. These are the models described in Table 2 of Marques et al. (2007). Table 5.7 of *Distance sampling: Methods and applications* does not discuss models with survey-specific detection functions. Note all of the models in the project have the same data filter applied to them; the filter truncates detections at 82.5m.

Drawing attention to the model named j10 – HN OBS MAS w82.5, this is the model chosen by AIC as the preferable model for this data set. The screen captures below show a) the appropriate checkboxes to have a common detection function across all strata and b) choosing the covariates for the model and treating observer as a factor covariate.

The first screenshot shows the 'Model Definition Properties' dialog box with the 'Estimate' tab selected. The 'Detection function' tab is also visible. The 'Stratum definition' section has 'Use layer type' selected with 'Stratum' as the layer type. The 'Sample definition' section has 'Use layer type' set to 'Sample'. The 'Quantities to estimate and level of resolution' table is as follows:

	Level of resolution of estimate		
	Global	Stratum	Sample
Density	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Encounter rate	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Detection function	<input checked="" type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Cluster size (if required)	<input type="checkbox"/>	<input checked="" type="checkbox"/>	<input type="checkbox"/>

The 'Global density estimate is' dropdown is set to 'Mean' and 'weighted by' is set to 'Stratum area'. The 'Name' field contains 'HR MCDS Obs MAS by strat'.

The second screenshot shows the same dialog box with the 'Detection function' tab selected. The 'Detection function covariates' table is as follows:

Layer type containing covariate	Field name of covariate	Factor	Cluster size
Observation	OBs	<input checked="" type="checkbox"/>	<input type="checkbox"/>
Observation	MAS	<input type="checkbox"/>	<input type="checkbox"/>

The 'Cluster size' section contains the following text: 'To include cluster size as a covariate, add the cluster size field to the table of covariates and tick the 'Cluster size' box in that row. When cluster size is a covariate, density is estimated using a different algorithm (see Help for details). Options are changed in the Estimate, Cluster Size and Variance tabs.'

All models can be fitted concurrently by highlighting multiple rows in the Project Browser and choosing the running man icon (fourth from right). With all 13 models from Table 5.7 of the book fitted (and a few extra thrown in), you can nearly duplicate Table 5.7.

By employing the final icon to the right in the *Analysis* tab menu, you can alter the columns that appear in the Results Browser to include/exclude results. Clicking on the header of any column in the results browser (such as *Delta AIC*) will sort the table on that column. The resulting table (below) matches the values shown in Table 5.7.

ID	Observer	Design	Name	# params	Delta AIC	ESW/EDR	GOF Chi-p	GOF CvM (cos) p	GOF K-S p	
150	1	2	7	d4 - Unicos by strat w82.5						
137	1	2	3	g6 - HN by strat w82.5						
136	1	2	1	e5 - HR by strat w82.5						
177	1	2	9	g7 - HR OBS MAS w82.5	5	0.00	45.54	0.000	0.400	0.036
141	1	2	4	h8 - HR OBS w82.5	4	1.73	45.30	0.000	0.300	0.003
182	1	2	14	i9 - HN Obs HAS by strat w82.5m	10	3.61	47.97	0.000	0.700	0.515
178	1	2	10	j10 - HN OBS MAS w82.5	6	5.53	47.92	0.000	0.600	0.410
181	1	2	13	k11 - HRpol OBS HAS w82.5	9	5.62	46.01	0.000	0.500	0.020
142	1	2	2	l12 - HN OBS w82.5	6	7.12	41.97	0.000	0.600	0.261
139	1	2	5	a1 - HN by strat f0 pooled w82.5	5	21.40	43.85	0.000	0.600	0.320
179	1	2	11	m13 - HN MAS w82.5	4	24.56	47.97	0.000	0.700	0.456
183	1	2	15	n14 - HN HAS by strat w82.5m	8	24.57	47.96	0.000	0.700	0.619
151	1	2	8	b2 - Unicos by strat f0 pooled w82.5	2	25.11	44.30	0.000	0.600	0.169
180	1	2	12	o15 - HR MAS w82.5	3	29.18	47.92	0.000	0.300	0.015
138	1	2	6	c3 - HR by strat f0 pooled w82.5	2	29.90	47.28	0.000	0.500	0.062
184	1	2	16	p16 - HRpol HAS w82.5	7	31.62	47.80	0.000	0.300	0.016

Figure 1:

2 Amakihi analysis in R

Analysis begins by acquiring the data from a comma-delimited file (this file was created by copying the data from the amakihi Distance project and removing a few columns.)

```
## Warning: package 'knitr' was built under R version 3.1.3
```

```
library(Distance)
amakihi <- read.csv(file="amakihi.csv")
scalemin <- sd(amakihi$MAS, na.rm = TRUE) # used in plotting
```

2.1 Exploratory data analysis

As discussed in Section 5.3.2.1, "it is important to gain an understanding of the data prior to fitting detection functions". With this in mind, preliminary analysis of distance sampling data involves

- assess the shape of the collected data,
- consider the level of truncation of detections, and
- explore patterns in potential covariates

```
par(mfrow=c(3,2))
hist(amakihi$distance, breaks=seq(0,260), main="", xlab = "Distance")
boxplot(amakihi$distance[!amakihi$OBS==""] ~ amakihi$OBS[!amakihi$OBS==""],
        xlab="Observer", ylab="Distance(m)")
hist(amakihi$distance[amakihi$distance<82.5], breaks=33,
     main="", xlab = "Distance")
plot(amakihi$MAS, amakihi$distance,
     xlab="Minutes after sunrise", ylab="Distance(m)",
     pch=19, cex=0.6)
abline(reg=lm(amakihi$distance~amakihi$MAS), lwd=2)
hist(amakihi$distance[amakihi$distance<82.5], breaks=10,
```

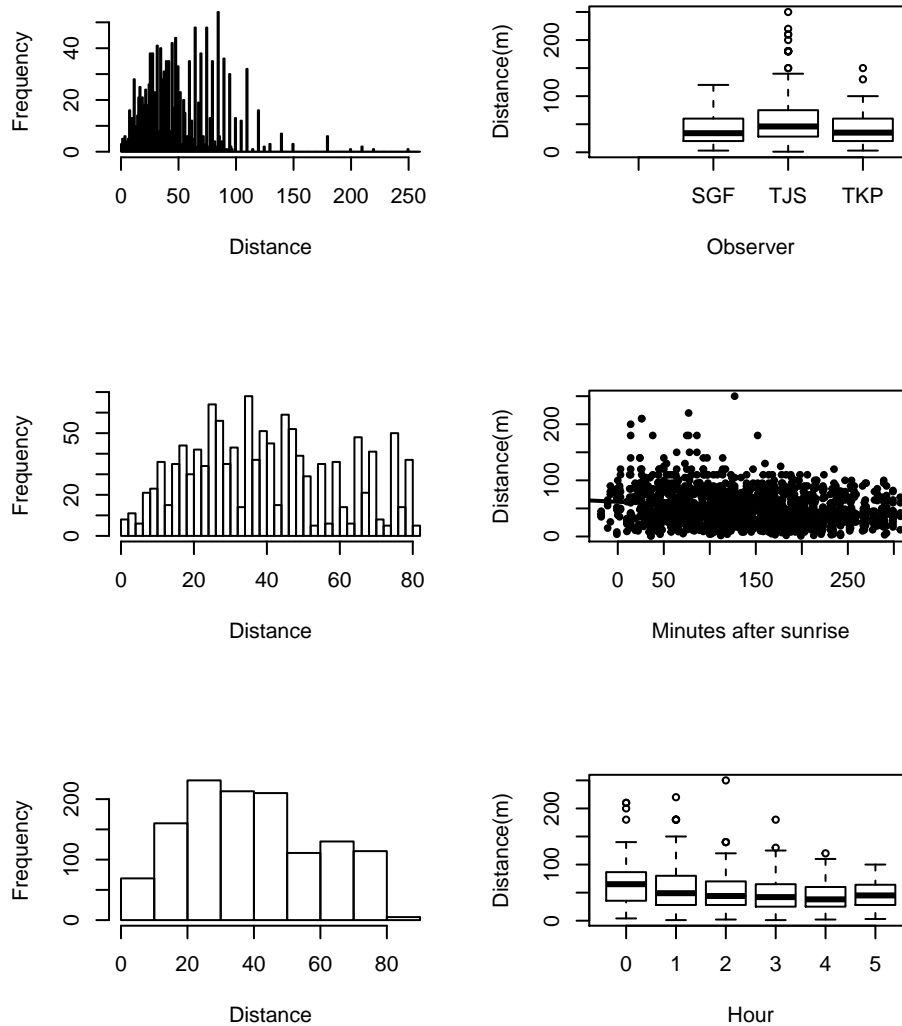


Figure 2: Exploratory data analysis of amakihi detections. Intended to duplicate Fig. 5.15 of book.

```
main="", xlab = "Distance")
boxplot(amakihi$distance~amakihi$HAS,
        xlab="Hour", ylab="Distance(m)")
```

```
par(mfrow=c(1,1))
```

2.2 Adjusting the raw covariates

Two adjustments need to be made to the covariates prior to analysis. Recall in the Distance project above, the *Factor* box was checked for the covariate OBS to indicate that the observer covariate was to be treated as a factor variable. When performing the analysis in R, you will note that OBS was read in as a factor variable because it consisted of characters

```
str(amakihi$OBS)
```

```
## Factor w/ 4 levels "", "SGF", "TJS", ...: 3 3 3 3 3 3 3 3 3 3 ...
```

however because HAS (hours after sunrise) was a numeric variable, it was read in as an integer. That is fine if we wish to include HAS in our model with the effect of HAS being monotonic (i.e., detectability either steadily increases or steadily decreases as a function of HAS). If we wish to allow HAS to have a non-linear effect on detectability, then we convert the integer HAS to a factor (this is how HAS was treated in the original analysis; have a look at model definition HN MCDS Obs HAS by strat in the Distance project).

```
amakihis$HAS <- as.factor(amakihis$HAS)
amakihis$OBS <- relevel(amakihis$OBS, ref="TKP")
amakihis$HAS <- relevel(amakihis$HAS, ref="5")
```

The final adjustment shown above, is to change the *reference* level of the *observer* and *hour* factor covariates. The only reason we use the `relevel()` function here is to get the estimated parameters in the detection function to match the parameters estimated by Distance.

More subtle is a transformation of the continuous covariate, MAS (minutes since sunrise). We are entertaining three possible covariates in our detection function: observer, hours and minutes since sunrise. Observer and hours are both factor variables, that we can think of as taking on values between 1 and 3 in the case of observer, and 1 to 6 in the case of hours. However minutes can take on values from -9 (detections before sunrise) to >300. The disparity in scales of measure between MAS and the other candidate covariates can lead to difficulties in the performance of the optimiser fitting the detection functions in R. The solution to the difficulty is to scale MAS such that is on a scale (-1 to 5) comparable with the other covariates.

Dividing all the MAS measurements by the standard deviation of those measurements accomplishes the desired compaction of the range of the MAS covariate without changing the shape of the distribution of MAS values.

```
amakihis$MAS <- amakihis$MAS/sd(amakihis$MAS, na.rm=TRUE)
```

2.3 Detection function fitting and goodness of fit

The Distance package in R can fit all of the models presented in Table 5.7 of the book. The function `ds()` performs the detection function fitting and in the `mrds` package, there is a function `ddf.gof()` that performs goodness of fit tests (in the form of χ^2 , Cramer von Mises and Kolmogorov-Smirnov tests).

2.3.1 Helper function

I built a convenient wrapper function to combine calls to both `ds()` and `ddf.gof()` in the same function. Motivation for this was to be able to duplicate Table 5.7 of the book.

```
fit.and.assess <- function(data=amakihis, key="hn",
                          adj="cos", order=NULL,
                          cov=c("MAS"), truncation=82.5,
                          plotddf = FALSE, ...) {
  # wrapper function to combine detection function fitting as well as
  # goodness of fit testing into a single function
  #
  # Input - name of dataframe, key/adjustment combination, order of adjustment terms,
  #         and a vector of covariates to include in detection function
  #         specifically for this example, I limit number of covariates to 2,
  #         truncation distance (default value for amakihis),
  #         flag plotddf to signal whether a plot of the detfn is required
  #
  # Output - named list containing the columns of Table 5.7 (with the exception
  #         of the effective detection radius). List will subsequently be
  #         post-processed to duplicate the table.

  if (length(cov)>2) stop("Function can take no more than 2 covariates")
  mystring <- ifelse(length(cov)==2,
                    paste(cov[1],cov[2],sep="+"),
```

```

        cov[1])
covariates <- as.formula(paste("~", mystring))
model.fit <- ds(data, key=key, adjustment=adj,
               formula=covariates, transect="point", order=order,
               truncation = truncation)
if (plotddf) plot(model.fit, pl.den=0, pch=19,
                 cex=0.7, main=paste(key, adj, cov))
aic <- model.fit$ddf$criterion
pars <- length(model.fit$ddf$par)
gof <- ddf.gof(model.fit$ddf)
chisq.p <- gof$chisquare$chi1$p
cvm.p <- gof$dsgof$CvM$p
ks.p <- gof$dsgof$ks$p
findings <- list(formula=mystring, key=key, aic=aic, pars=pars,
                 chisq.p=chisq.p, cvm.p=cvm.p, ks.p=ks.p)
return(findings)
}

```

2.3.2 Candidate models

It is not best practice to take a scattergun approach to detection function model fitting, but the candidate model set is presented in Table 5.7 of the book, the straightforward way to fit the 13 models is to make 13 calls to the helper function just described:

```

hour.hn <- fit.and.assess(key="hn", order=2, cov=c("HAS"))
hour.hr <- fit.and.assess(key="hr", adj=NULL, cov=c("HAS"))
obs.hour.hn <- fit.and.assess(key="hn", order=0, cov=c("OBS","HAS")) # fails if order>0
obs.hour.hr <- fit.and.assess(key="hr", adj=NULL, cov=c("OBS","HAS"))
obs.min.hn <- fit.and.assess(key="hn", order=0, cov=c("OBS","MAS")) # fails if order>0
obs.min.hr <- fit.and.assess(key="hr", adj=NULL, cov=c("OBS","MAS"))
min.hn <- fit.and.assess(key="hn", order=0, cov=c("MAS")) # fails if order>0
min.hr <- fit.and.assess(key="hr", adj=NULL, cov=c("MAS"))
obs.hn <- fit.and.assess(key="hn", order=0, cov=c("OBS")) # fails if order>0
obs.hr <- fit.and.assess(key="hr", adj=NULL, cov=c("OBS"))
hn <- fit.and.assess(key="hn", order=(2:5), cov=c(1))
hr <- fit.and.assess(key="hr", adj=NULL, cov=c(1))
uni <- fit.and.assess(key="uni", cov=c(1))

```

Note the use of the `cov=c(1)` notation to choose to fit a model with no covariates.

2.3.3 Summarise model selection

We gather results of 13 model fits into a single data frame, using a function found in the `data.table` package to bind together lists into rows of a dataframe.

```

library(data.table)
library(knitr)
mymodels <- list(hour.hn, hour.hr, obs.hour.hn, obs.hour.hr,
                obs.min.hn, obs.min.hr, min.hn, min.hr,
                obs.hn, obs.hr, hn, hr, uni)
results.frame <- rbindlist(mymodels)
results.frame <- results.frame[order(results.frame$aic), ] # sort by increasing AIC
smallest <- results.frame[1, aic] # note syntax for data.table
results.frame$deltaaic <- results.frame$aic - smallest
setcolorder(results.frame, c("formula","key","pars","deltaaic","chisq.p","cvm.p","ks.p","aic"))
kable(results.frame[,.(formula, key, pars, deltaaic, chisq.p, cvm.p, ks.p)], digits=c(0,0,0,1,0,3,3))

```

Table 1: Attempt to duplicate Table 5.7 using R function `ds` from the Distance package.

formula	key	pars	deltaaic	chisq.p	cvm.p	ks.p
OBS+MAS	hr	5	0.0	0	0.389	0.076
OBS	hr	4	1.1	0	0.270	0.025
OBS+HAS	hr	9	5.8	0	0.450	0.084
1	hn	5	21.7	0	0.557	0.338
OBS+HAS	hn	8	23.7	0	0.011	0.028
1	uni	2	25.4	0	0.440	0.169
OBS+MAS	hn	4	26.5	0	0.008	0.025
MAS	hr	3	28.3	0	0.558	0.256
1	hr	2	30.2	0	0.334	0.063
HAS	hr	7	30.8	0	0.580	0.291
HAS	hn	7	35.5	0	0.228	0.164
OBS	hn	3	39.1	0	0.003	0.001
MAS	hn	2	49.2	0	0.007	0.020

Duplication of Table 5.7 is not exact. The main discrepancy lies in that the R function `ds()` has convergence challenges with adjustment terms and covariates in detection functions. That is not a problem for the amakihi hazard rate key function models (they did not use adjustment terms). But the half-normal key functions employed adjustment terms in the original Marques et al. (2007) analysis. Models OBS+HAS, OBS+MAS, OBS and MAS with a half-normal key function all failed to converge, so they were fitted without adjustment terms. In each model, the model without adjustments had AIC scores >20 AIC units larger than the same models that included adjustments (fitted in Distance for Windows). As a consequence, models that should have had adjustment terms are models with the two largest AICs, while OBS+HAS should have AIC values of 3.6 rather than 23.7 and OBS+MAS should have AIC values of 5.5 rather than 26.5; if a more robust optimisation engine were available in R. Note also that the Cramér von Mises goodness of fit P-value is very small for the models fitted without adjustment terms.

2.3.4 Inference from best model

The model with the lowest AIC used the hr key function with covariates OBS+MAS. The shape of the detection function is

```
bestmod <- ds(amakihi, trunc=82.5, key="hr", adj=NULL, formula=~OBS+MAS)
pred.haz.obs.minute <- function(pars, trunc=82.5, obs2=0, obs3=0, mas=0) {
  # creates hazard rate detection function for plotting
  # based upon parameters of detection function and covariate values
  # tailored for the OBS+MAS covariate model
  distances <- seq(0, trunc, length=100)
  nu <- pars[2] + pars[3]*obs2 + pars[4]*obs3 + pars[5]*mas
  sigma <- exp(nu)
  mycurve <- 1-exp(-(distances/sigma)^-pars[1])
  return(mycurve)
}
par(mfrow=c(1,2))
dists <- seq(0, 82.5, length.out = 100)
obs1.min0 <- pred.haz.obs.minute(bestmod$ddf$par)
obs2.min0 <- pred.haz.obs.minute(bestmod$ddf$par, obs2=1)
obs3.min0 <- pred.haz.obs.minute(bestmod$ddf$par, obs3=1)
plot(dists, obs1.min0, type='l', ylim=c(0,1),
     ylab="Detection probability by OBS", xlab="Distance (m)")
lines(dists, obs2.min0, lty=2)
lines(dists, obs3.min0, lty=3)

obs1.0 <- pred.haz.obs.minute(bestmod$ddf$par)
obs1.60 <- pred.haz.obs.minute(bestmod$ddf$par, mas=60/scalemin)
```

```

obs1.120 <- pred.haz.obs.minute(bestmod$ddf$par,mass=120/scalemin)
obs1.180 <- pred.haz.obs.minute(bestmod$ddf$par,mass=180/scalemin)
obs1.240 <- pred.haz.obs.minute(bestmod$ddf$par,mass=240/scalemin)

plot(dists, obs1.0, type='l', ylim=c(0,1),
     ylab="Detection probability by MAS", xlab="Distance (m)")
lines(dists, obs1.60)
lines(dists, obs1.120)
lines(dists, obs1.180)
lines(dists, obs1.240)

```

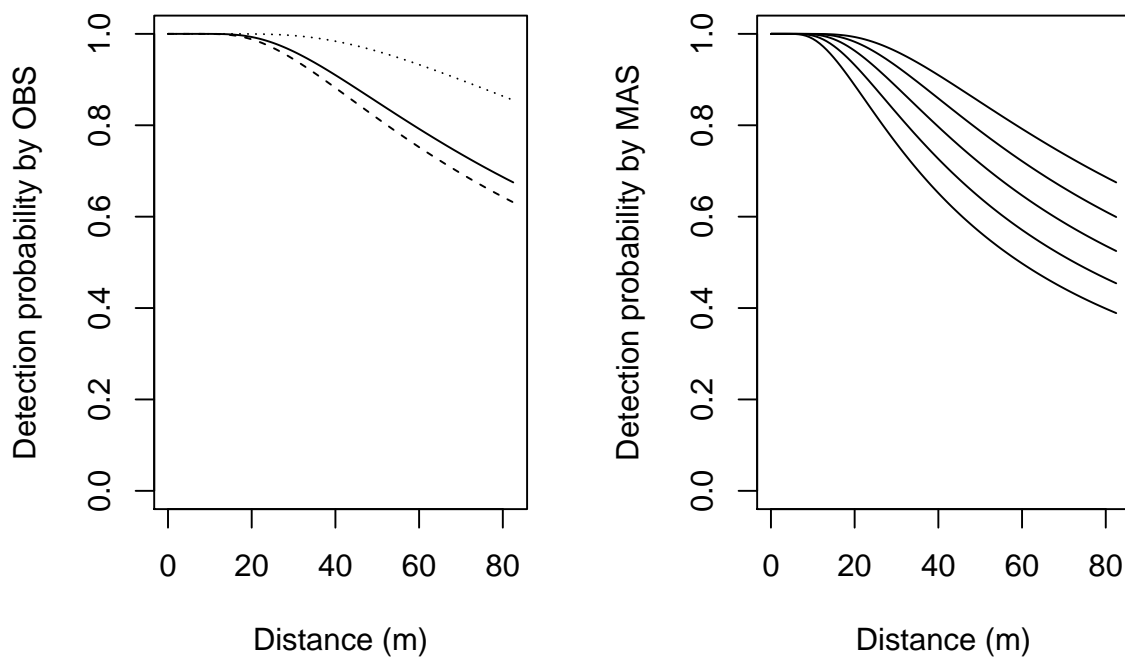


Figure 3: Hazard rate detection function plotted for three observers in the Amakihi study (left) and for Observer1 and sunrise, 1, 2, 3 and 4 hours after sunrise. Based on model with OBS+MAS as covariates.

```
par(mfrow=c(1,1))
```

References

Marques, T. A., L. Thomas, S. G. Fancy, and S. T. Buckland. 2007. Improving estimates of bird density using multiple covariate distance sampling. *The Auk* 124:1229–1243.

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